Direct determination of mean-field from data on matter density

M. R. Anders, S. Shlomo, and I. Talmi¹ ¹Weizmann Institute of Science, Rehovot, Israel

In this work we consider the single particle Schrodinger equation and develop a method for determining the single particle potential V from a given single particle wave function $\Psi(\vec{r})$ or matter density, assuming it is known for all \vec{r} . In particular, we consider the case of spherical symmetry. The results of this work are very important for investigation of the validity of the shell model and for the development of a modern EDF which provides enhanced predictive power for properties of nuclei and the equation of state (EOS) of nuclear matter (NM).

For the single particle Schrodinger equation,

$$-\frac{\hbar^2}{2m}\Delta\Psi + V\Psi = E\Psi, \qquad (1)$$

we have that for a given single particle wave function $\Psi(\vec{r})$, known for all \vec{r} , the corresponding single particle potential V is uniquely determined [1] from

$$V(\vec{r}) = E + \frac{\hbar^2}{2m} \frac{\Delta \Psi(\vec{r})}{\Psi(\vec{r})}.$$
(2)

Note that for a nonsingular V, $\Delta \Psi(\vec{r}) = 0$ when $\Psi(\vec{r}) = 0$. In the spherical case we have for the centroid potential

$$V_{cen}(r) = E + \frac{\hbar^2}{2m} \frac{d^2 R_{nlj}}{dr^2} \frac{1}{R_{nlj}(r)} - \frac{\hbar^2}{2m} \frac{l(l+1)}{r} - \frac{1}{2} (1 - \tau_z) V_{coul}(r) - c_{ls} V_{s.o.}(r) .$$
(3)

Here, $V_{cen}(r)$, $\vec{s} \cdot \vec{l} V_{s.o.}(r)$ and $\frac{1}{2}(1 - \tau_z)V_{coul}(r)$, are the central, spin-orbit and coulomb potentials, respectively, and $\tau_z = 1$ for a neutron and -1 for a proton.

We consider, in particular, the charge density difference, $\Delta \rho_c(r)$, between the isotones ²⁰⁶Pb – ²⁰⁵Tl, associated with the proton 3S_{1/2} single particle orbit, and determine the corresponding single particle potential. The experimental data for the charge densities, $\rho_c(r)$, of the isotones ²⁰⁶Pb and ²⁰⁵Tl, obtained from accurate elastic electron scattering experiments, are taken from Ref. [1]. In Fig. 1a we present the experimental data for the charge density difference, $\Delta \rho_c(r)$, between the isotones ²⁰⁶Pb – ²⁰⁵Tl, shown by the dashed line. It is normalized to a total charge of one proton (Z=1). The dotted lines indicate the experimental uncertainty. Note that the two nodes associated with the proton 3S_{1/2} orbit are clearly seen in the figure. To extract the corresponding single particle potential we need the point proton distribution, $\Delta \rho_p(r)$. This is obtained by determining the point proton form factor, $F_p(q)$, and then extracting $\Delta \rho_p(r)$. The results are shown in Fig. 1b. Note that $\Delta \rho_p(r)$ (dashed line) is slightly negative at the first node (at

~2.6 fm) and above zero at the second node (r~4.9 fm). Using these results we determine the corresponding mean field associated with the $3S_{1/2}$ orbit in ²⁰⁶Pb [2].

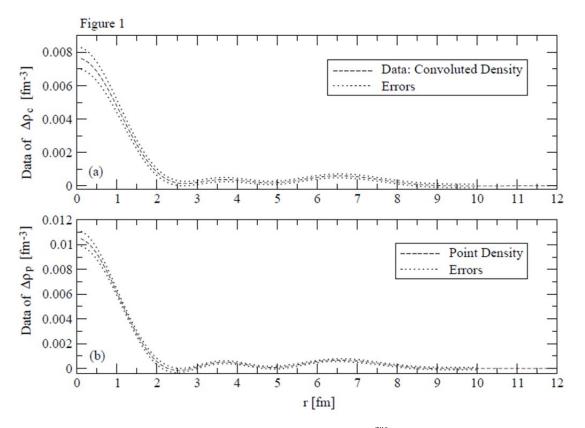


FIG. 1. Charge density (a) and point density (b) for the $3_{S1/2}$ orbit in ²⁰⁶Pb.

- [1] J.M. Cavedon et al., Phys. Rev. Lett. 49, 978 (1982).
- [2] M.R. Anders, S. Shlomo and I. Talmi, in preparation.